

Fate of the spectator Higgs during and after inflation

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inflation

$$H_* \approx \text{const.}$$

dynamics unknown (slow rolling scalar(s)?)

light **scalar spectators** (might) exist

$$m \ll H_*$$

$$\rho_\sigma \ll \rho_{\text{inf}}$$

example: the **higgs**

contents:

spectator Higgs dynamics

1. during

2. after inflation

**3. when coupled
 to inflaton**

DURING INFLATION

(near) massless scalars in an expanding background



stochastic treatment

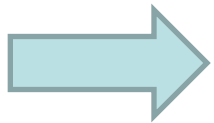
(cf. Starobinsky)

Langevin (simplified):

decompose field into UV and IR parts:

$$\Phi_{IR} \propto \int dk W(k, t) \phi_k(t)$$

$$W(k, t) = \theta(k - xaH)$$



$$\dot{\Phi}_{IR} = -\frac{\partial}{3H\partial\Phi} V(\Phi_{IR}) + s(x, \eta)$$

$k \ll aH$

stochastic term, white noise correlators

$$\langle SS \rangle(dN) = (1 + x^3) \frac{H^2 dN}{4\pi^2}, \quad k = xa(N)H$$

N = # efoldings

inflationary fluctuations

variance of massless field spreads out

$$\langle \phi^2 \rangle = \frac{1}{4\pi^2} H^2 N$$

$N = \#$ of e-folds

evolution of pdf: Langevin \rightarrow Fokker-Planck

$$\frac{\partial P}{\partial t} = \frac{1}{3H} \frac{\partial}{\partial \phi} [V'(\phi)P] + \frac{H^3}{8\pi^2} \frac{\partial^2}{\partial \phi^2} P$$

equilibrium pdf:

$$P \propto \exp(-8\pi^2 V / 3H^4)$$

not in slow roll?

Moss, Rigopoulos

equilibrium pdf:

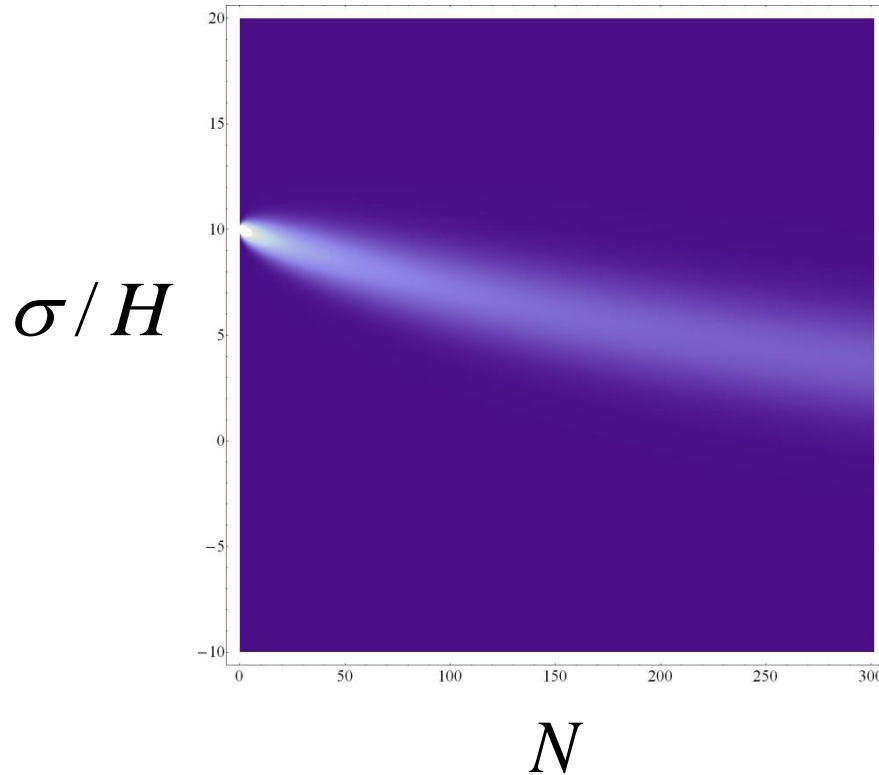
$$P \propto \exp \left[-8\pi^2 \left(\frac{1}{2} v^2 + V \right) / 3H^4 \right]$$

(Gaussian window)

$$v = \dot{\phi}$$

v equilibrates at the time scale $\Delta t = H^{-1}$

EQUILIBRATION TIME



example

$$V = \frac{1}{2} m^2 \sigma^2$$

$$m = 0.01H$$

KE, Lerner, Taanila, Tranberg

relaxation time

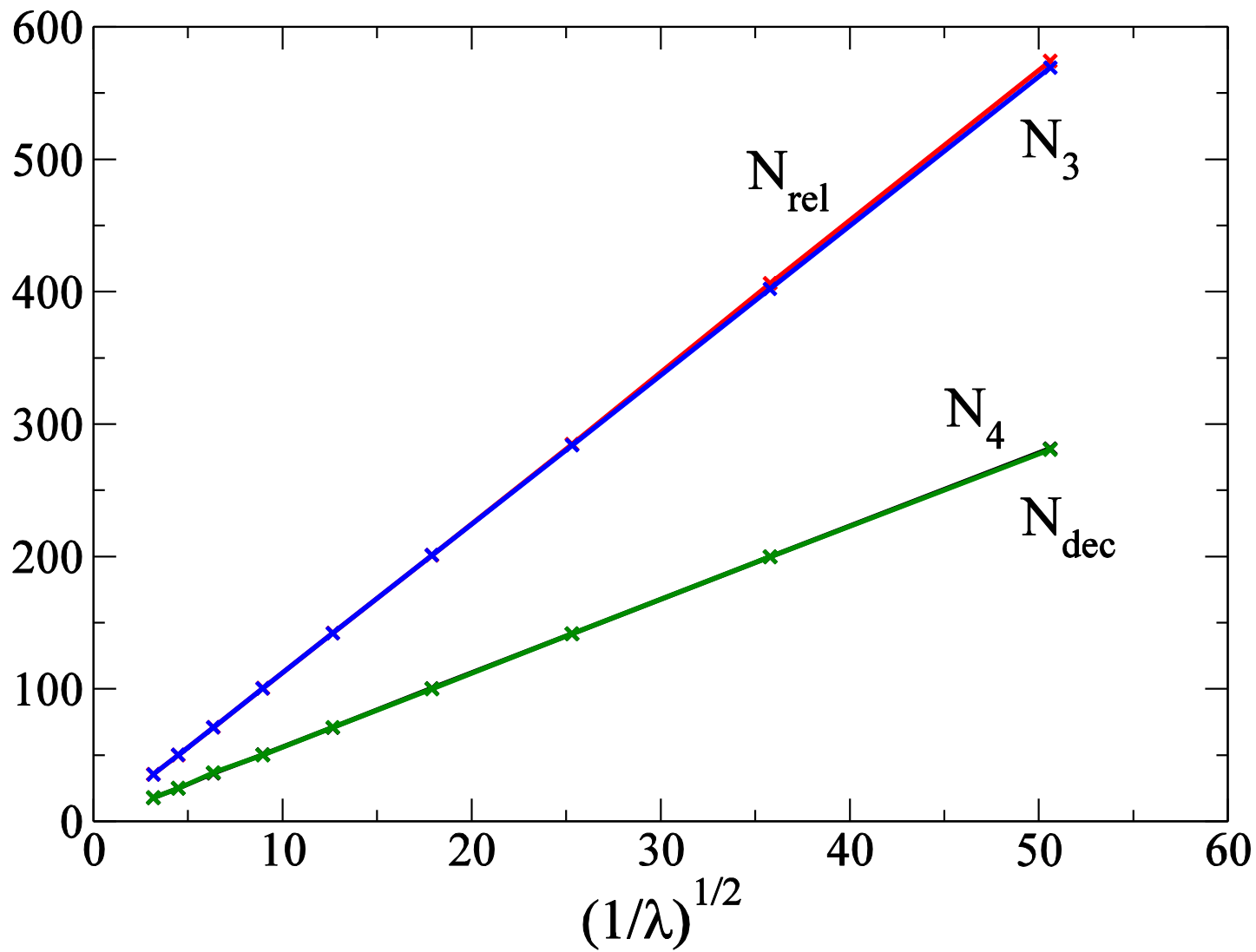
$$N_{rel} = \frac{3H_*^2}{m^2}$$

moving

decoherence time

$$N_{dec} = \frac{3H_*^2}{2m^2}$$

spreading



quartic potential

$$V = \frac{1}{4} \lambda \phi^4$$

relaxation time

$$N_{rel} \approx \frac{11.3}{\sqrt{\lambda}}$$

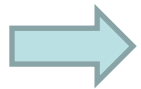
decoherence time

$$N_{dec} \approx \frac{5.65}{\sqrt{\lambda}}$$

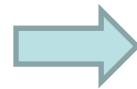
Example: the higgs

$$V \approx \frac{1}{4} \lambda h^4$$

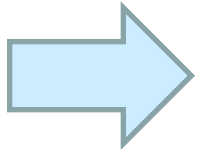
RGE $\rightarrow \lambda \approx 0.01$ at inflationary scales (?)



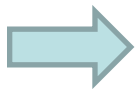
decoherence at ~ 60 efolds



mean field from equilibrium dist



$$h_* \approx 0.36 \lambda^{-1/4} H_* \approx 1.1 H_*$$



effective higgs mass

$$m_{h_*}^2 \approx V''(h_*) = 0.40 \lambda^{1/2} H_*^2 = 0.04 H_*^2$$

the Higgs

at equilibrium after inflation:

$$h_* \approx 0.36\lambda^{-1/4} H_* \approx 1.1H_*$$

"typical value"

how does the condensate decay?

1. inflaton decays first \rightarrow thermal background
(assuming thermalization)

more complicated

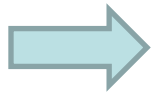
2. Higgs decays first (in matter dominated universe)

after inflation

MATTER DOMINATION

Higgs starts to move ... and becomes effectively massive at

$$\frac{H_{\text{osc}}}{H_*} \sim \frac{1}{4} \lambda_*^{3/4}$$



oscillations

$$t_{\text{osc}} \lesssim \mathcal{O}(10^2) H_*^{-1}$$

**decay rates depend on the value
of the Higgs background field**

perturbative decays

to gauge bosons: kinematically blocked until

$$t \sim \lambda(H_*)^{-3/8} \left(\frac{H_*}{10^2 \text{ GeV}} \right)^{3/2} H_*^{-1} \quad \text{not efficient unless } H_* \ll 10^5 \text{ GeV.}$$

to fermions: top channel kinematically blocked, others ok

$$\Gamma(h \rightarrow bb) = \frac{3\sqrt{3}\lambda y_b^2 h_{\text{osc}}}{16\pi} \left(1 - \frac{2y_b^2}{3\lambda} \right)^{3/2} \sim 10^{-6} \lambda_*^{3/4} H_*$$

takes $\gg 10^6$ Hubble times

not efficient

non-perturbative decays

KE, Nurmi, Rusak

resonant production of gauge bosons

W's in the unitary gauge:

(abelian approx.)

$$\ddot{W}_\mu^\pm(z, k) + \omega_k^2 W_\mu^\pm(z, k) = 0, \quad \omega_k^2 = \frac{k^2}{a^2 \lambda h_{\text{osc}}^2} + q_W \frac{h(z)^2}{h_{\text{osc}}^2} + \Delta.$$

$$q_W = \frac{m_W^2(t)}{\lambda h^2(t)} = \frac{g^2}{4\lambda}$$

 = 0 for matter domination

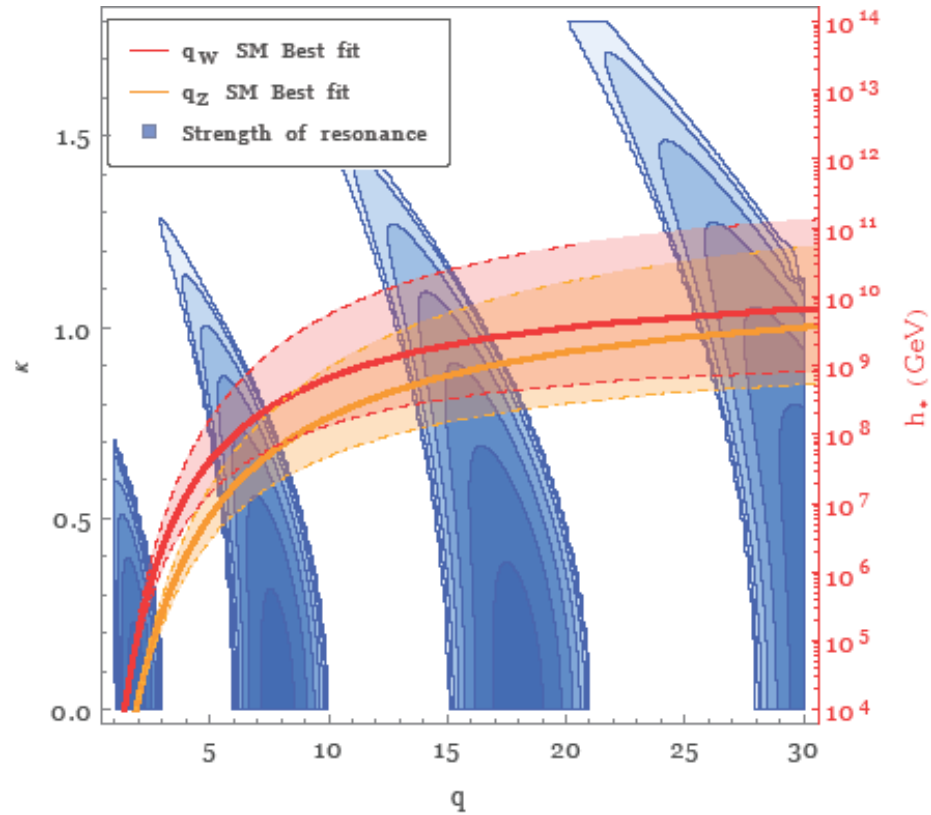
Higgs eq of motion

$$\frac{\ddot{h}}{h_{\text{osc}}} + 3 \frac{H}{\sqrt{\lambda} h_{\text{osc}}} \frac{\dot{h}}{h_{\text{osc}}} + \left(\frac{h}{h_{\text{osc}}} \right)^3 = 0$$

abelian estimate:

H_*/GeV	λ	$H_{\text{osc}}/H_{\text{dec}}$	n_ϕ^{dec}
10^4	0.09	370	1 000
10^6	0.04	360	1 700
10^8	0.02	630	5 100
10^{10}	0.005	340	7 700

resonance structure



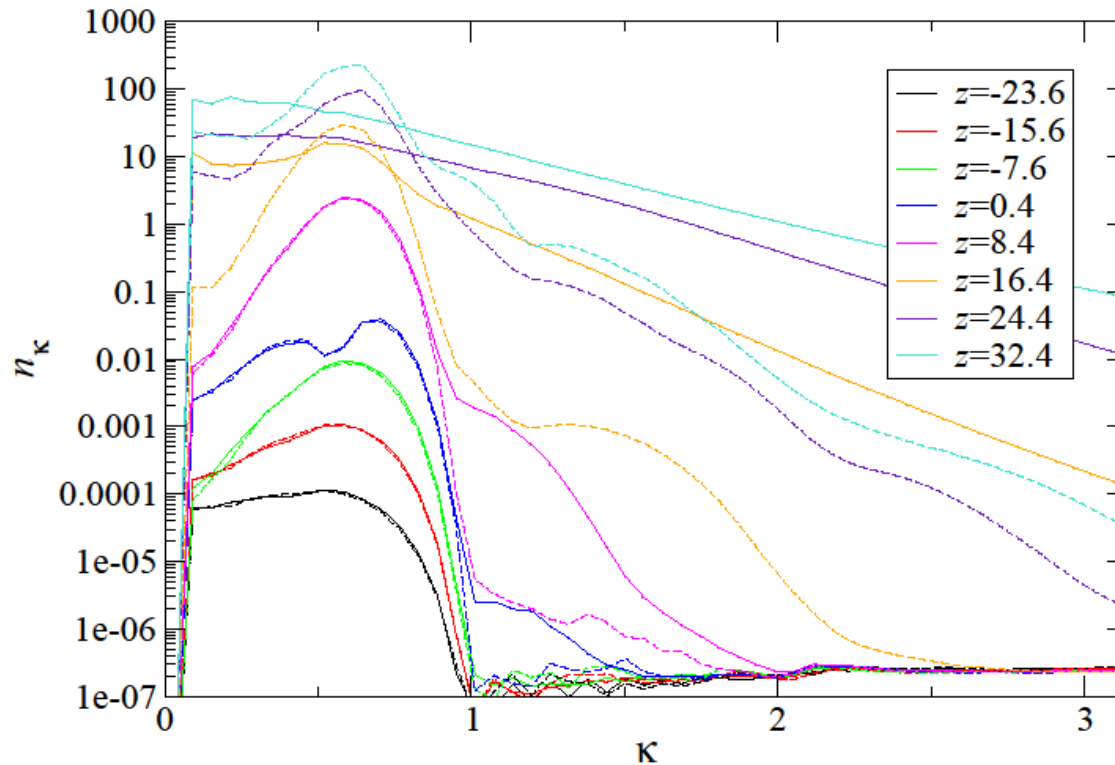
for SM, the resonance is broadish

best fit SM: $q_W = 18$, $q_Z = 29$

non-abelian terms matter

KE, Nurmi, Rusak, Weir

SU(2) on lattice



$$z = (\lambda_h (ah)_{osc}^2)^{1/2} (\tau - \tau_{osc})$$

$$\kappa^2 = \frac{k^2}{\lambda_h (ah)_{osc}^2}$$

abelian: dashed

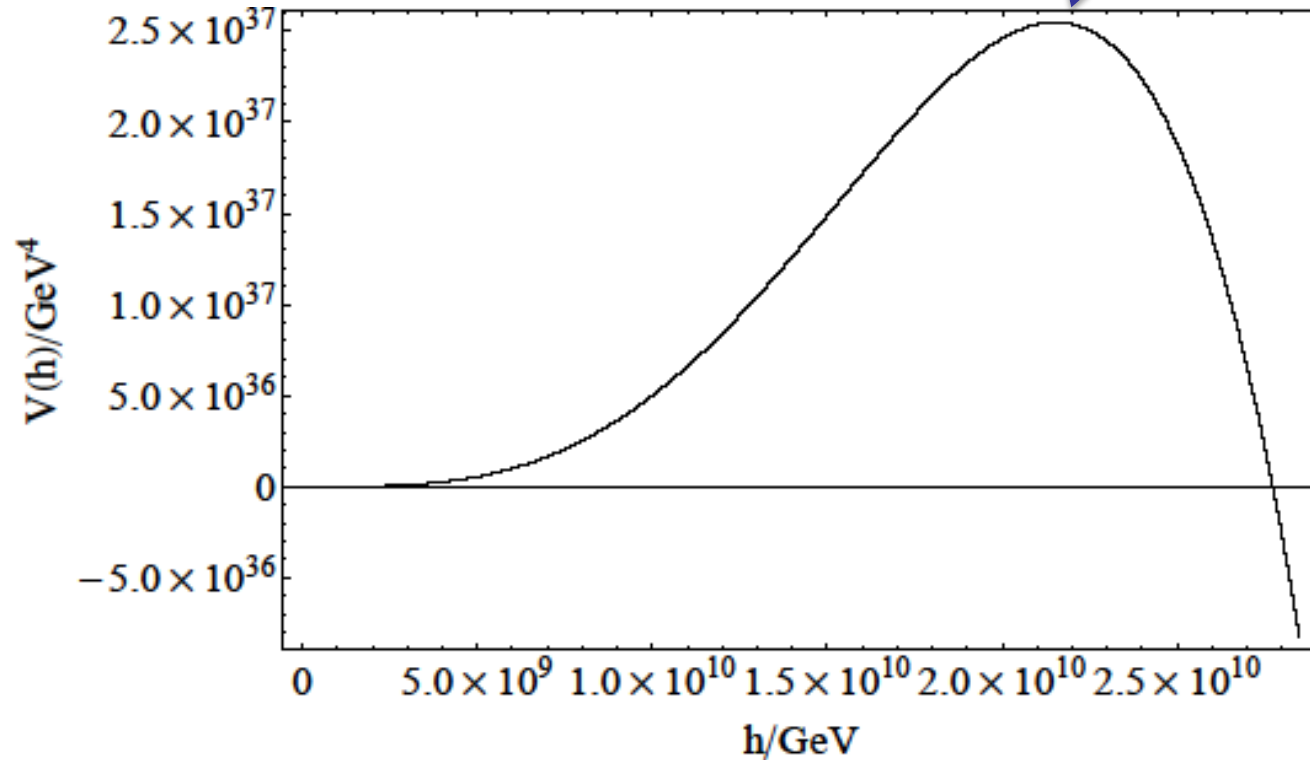
non-abelian: solid

non-abelian interactions destroy effectively the Higgs condensate

Higgs vacuum instability

fluctuate over the top? – very bad

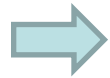
very sensitive to RGE



$$\lambda(h_{\max}) + \frac{\beta(h_{\max})}{4} = 0$$

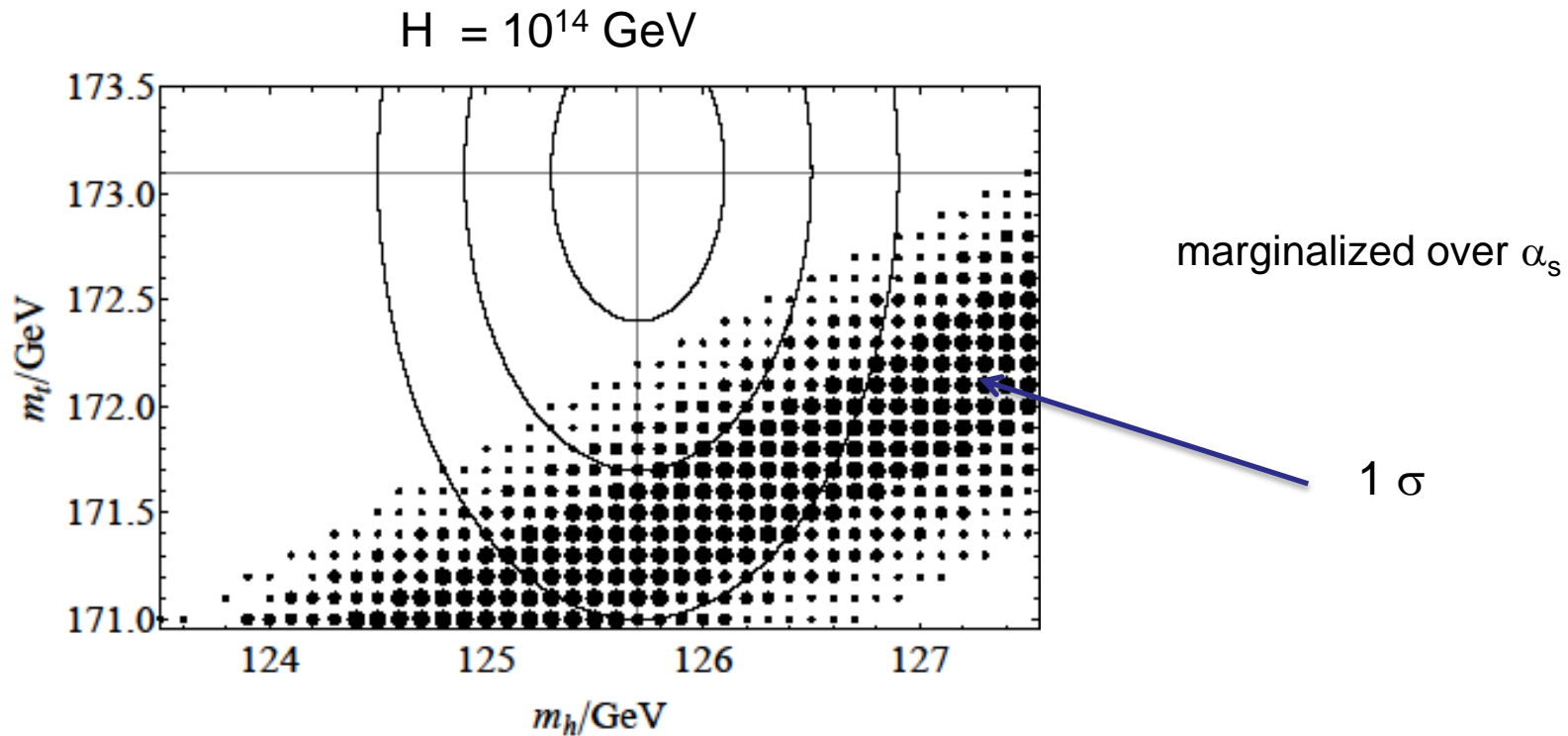
Espinosa, Giudice, Riotto
Kobakhidze, Spencer-Smith
KE, Meriniemi, Nurmi

fluctuations in kinetic energy $\sim H^4$



wrong vacuum unless $V > H^4$

→ possible problems for high inflationary scale



Coupling the Higgs and the inflaton

Reheating \rightarrow ... \rightarrow Standard Model \supset **Higgs**



loop induced Higgs-inflaton couplings

even tiny ones matter!

Coupling the Higgs and the inflaton

KE, Lebedev, Karciauskas, Rusak, Zatta

$$L = L_{chaotic}(\phi) + L_{higgs}(h) - \frac{1}{4} \lambda_{h\phi} h^2 \phi^2 - \frac{1}{2} \sigma_{h\phi} \phi h^2$$

$$m = 1.3 \times 10^{-6} M_{Pl}$$

$$V = \frac{1}{4} \lambda_h (h) h^4$$

inflaton oscillates $\phi = \Phi(t) \cos(mt)$

$$\Phi(t) \approx (3\pi)^{-1/2} \frac{M_{Pl}}{mt}, \quad \Phi(t) < \Phi_0 = 0.2 M_{Pl}$$



oscillating Higgs mass

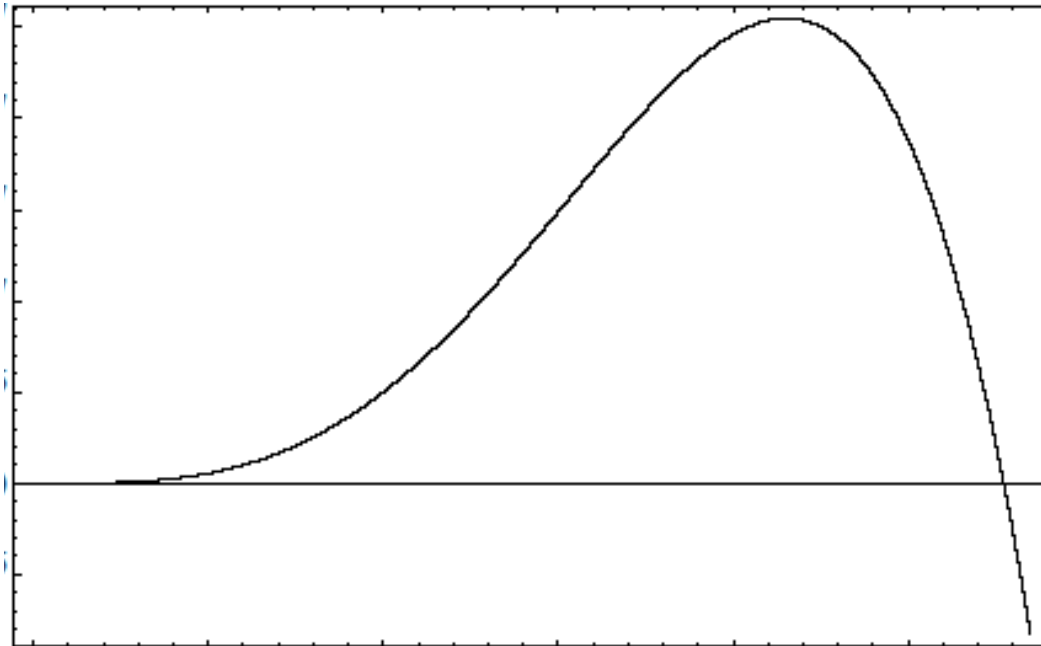
resonant excitation of Higgs modes h_k



$\langle h^2 \rangle$ over the top?

$$h_c \approx 10^{10} \text{ GeV}$$

$V(h)/\text{GeV}^4$



some constraints

$$10^{-10} < \lambda_{h\phi} < 10^{-6} \quad \text{eff mass} > H, \text{ flatness of potential}$$

$$\lambda_{h\phi} \phi^2 \gg \sigma_{h\phi} \phi \quad \text{effective mass not dependent on the sign of inflaton field}$$

(A) neglect trilinear coupling



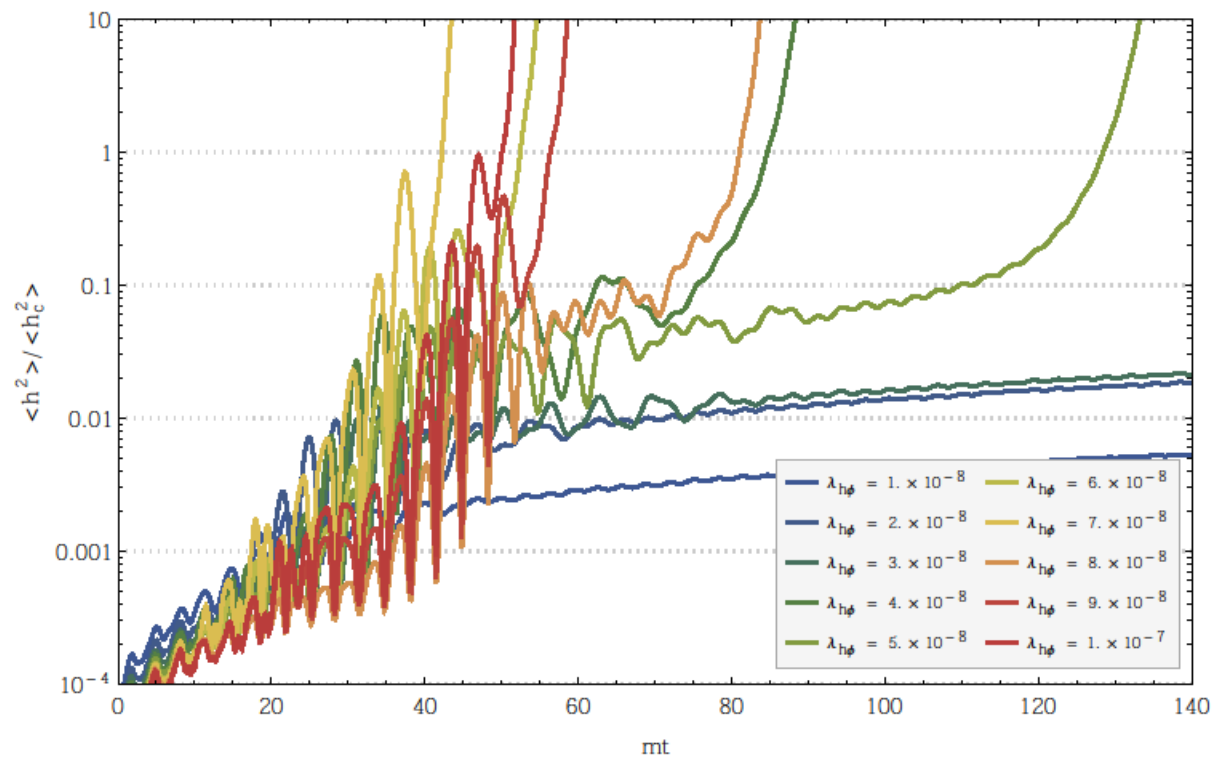
broad parametric resonance

Hartree approximation $h^4 \rightarrow 6h^2 \langle h^2 \rangle$

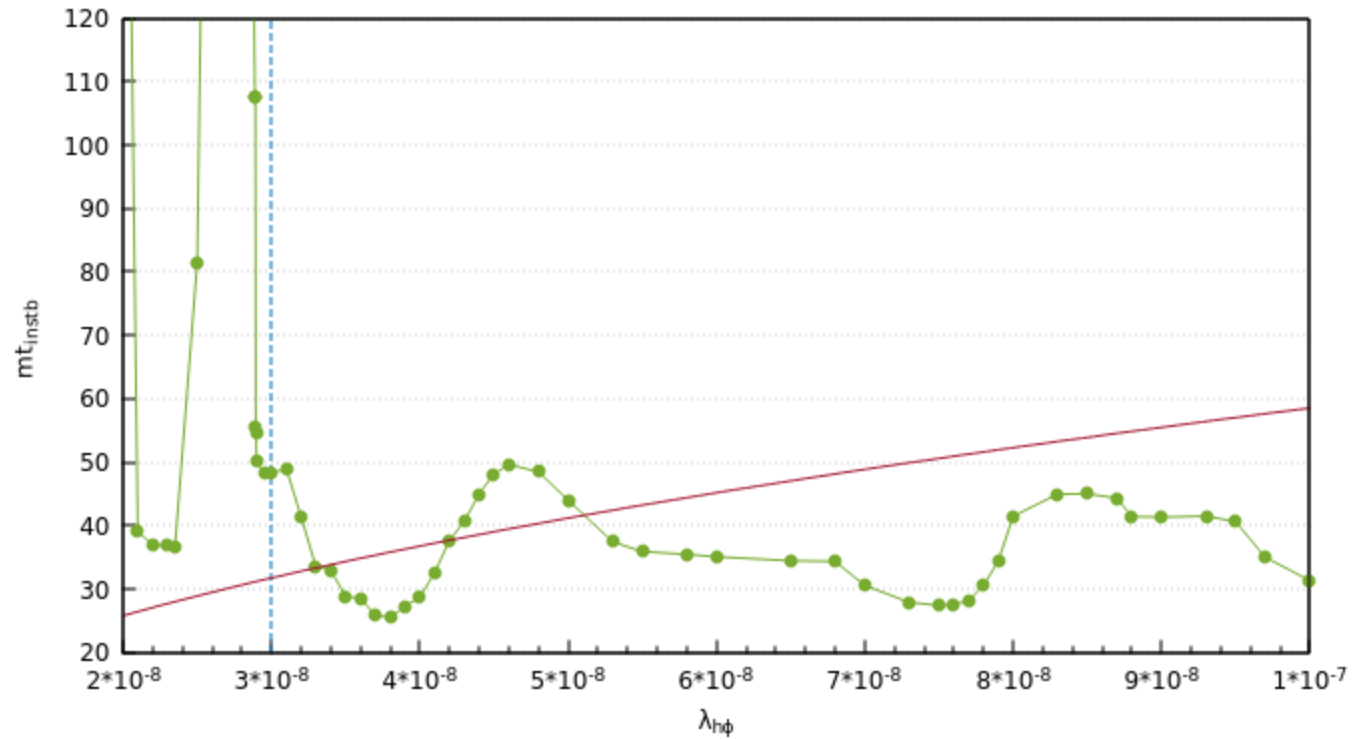


$$\omega_k^2 = \frac{k^2}{a^2} + \frac{1}{2} \lambda_{h\phi} \Phi^2 \cos^2(mt) + 3\lambda_h a^{-3} \langle X^2 \rangle$$

$$X_k = a^{3/2} h_k$$



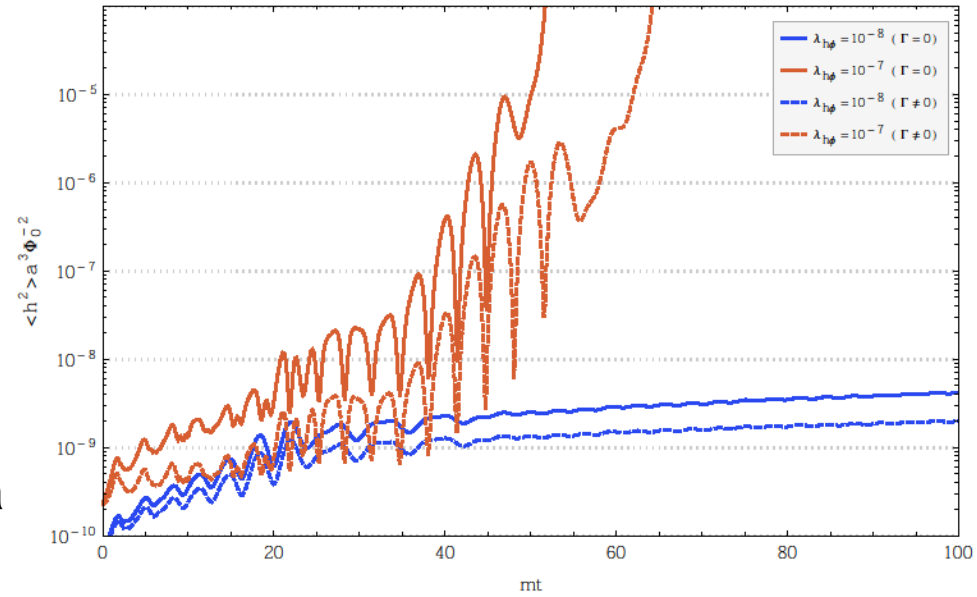
beyond Hartree approximation: LATTICEEASY



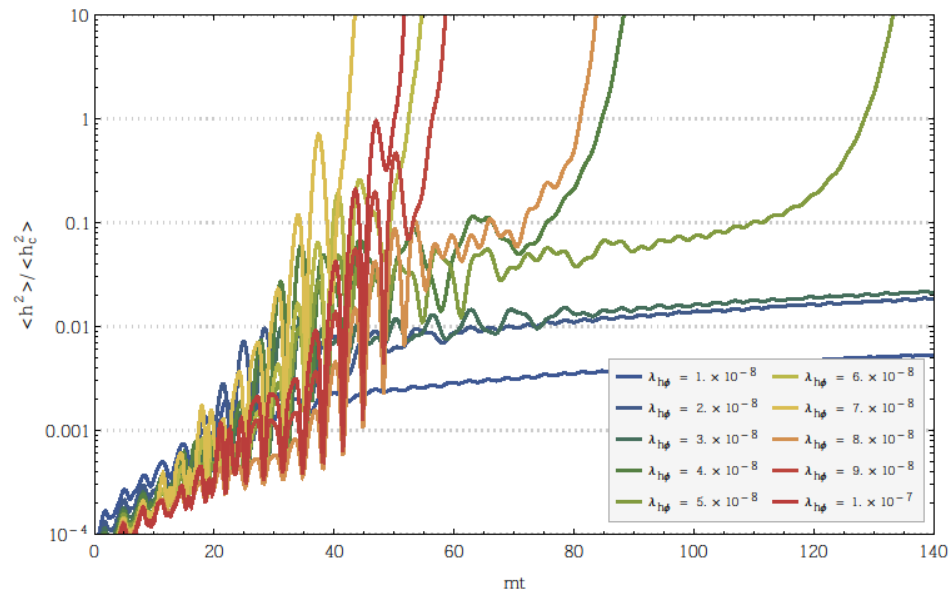
← vacuum instability

with $h \rightarrow \text{top}$

reduces Higgs quanta
by ~ 2



without



(B) switch on trilinear coupling



tachyonic instability

$$\omega_k^2 = \frac{k^2}{a^2} + \sigma_{h\phi} \Phi \cos(mt) + \frac{1}{2} \lambda_{h\phi} \Phi^2 \cos^2(mt) + 3\lambda_h a^{-3} \langle X^2 \rangle$$



p



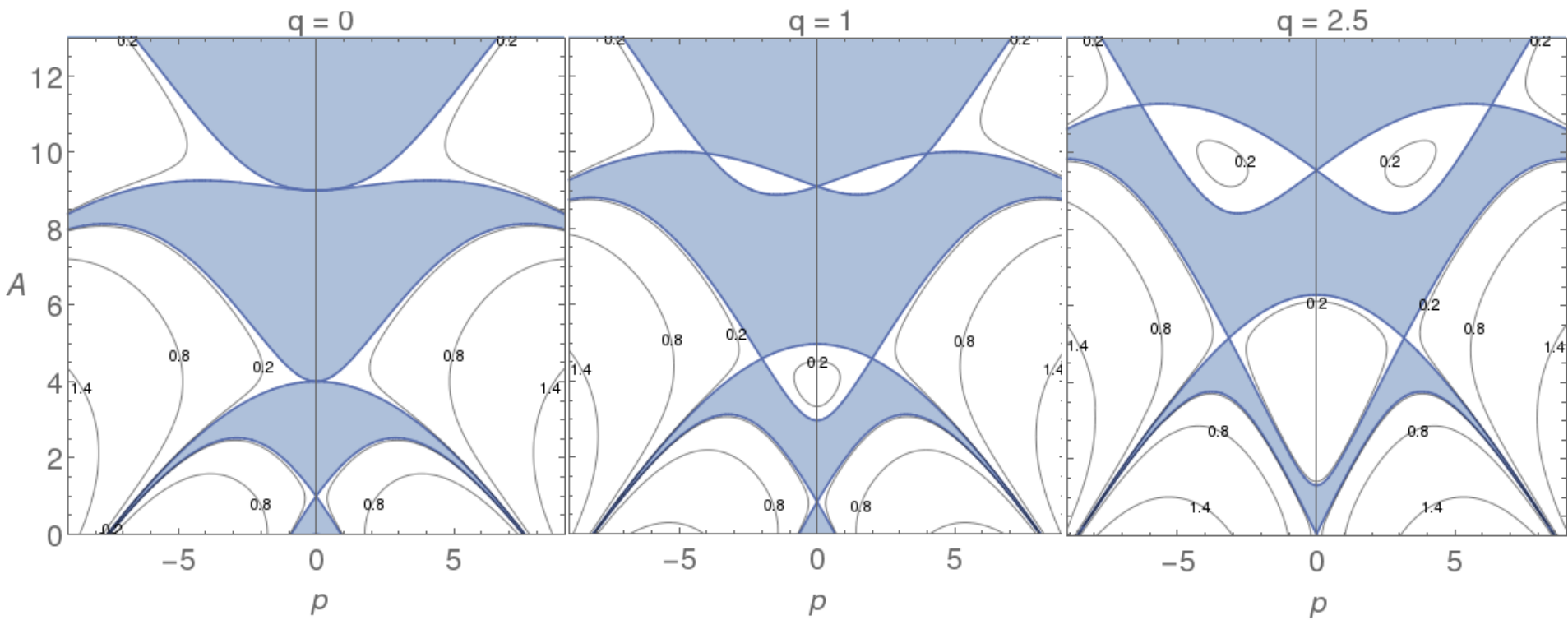
q

$$X_k = a^{3/2} h_k$$



Whittaker-Hill (= complicated Mathieu)

recipe: choose stable vacuum, switch on σ (sign also matters)

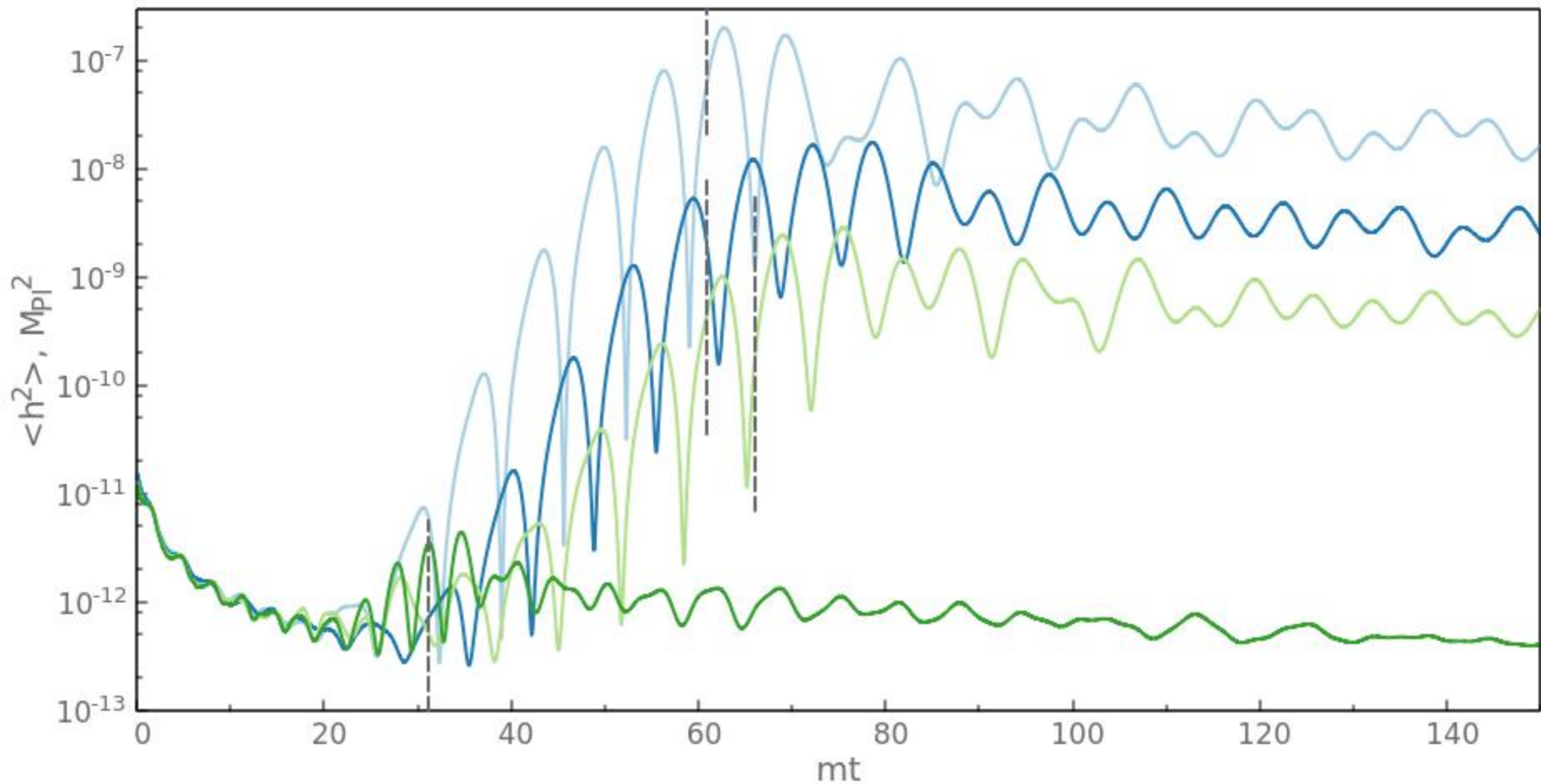


Whittaker-Hill stability bands

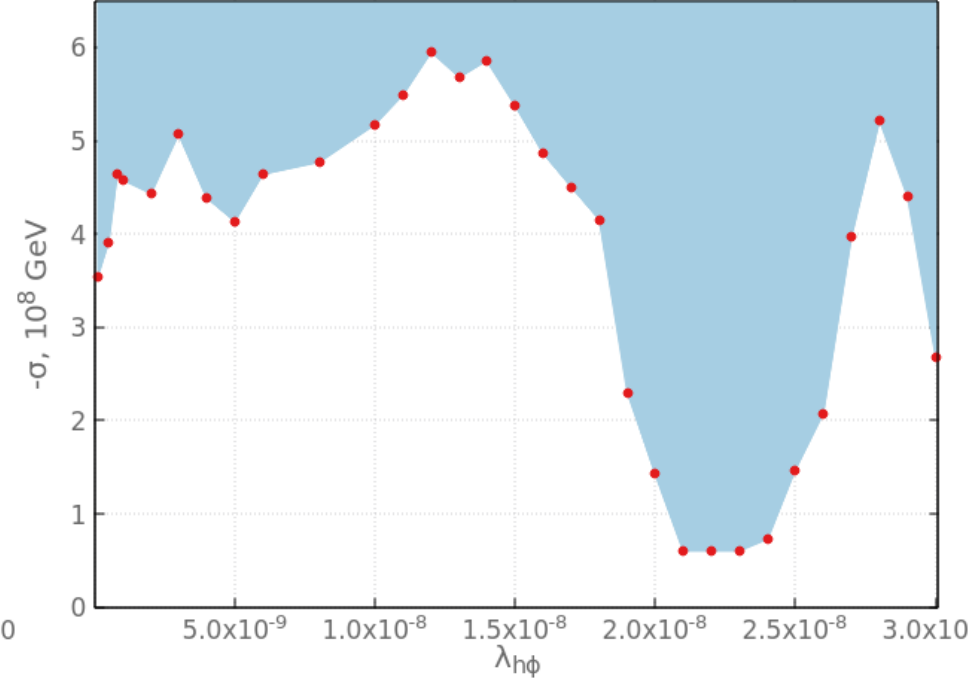
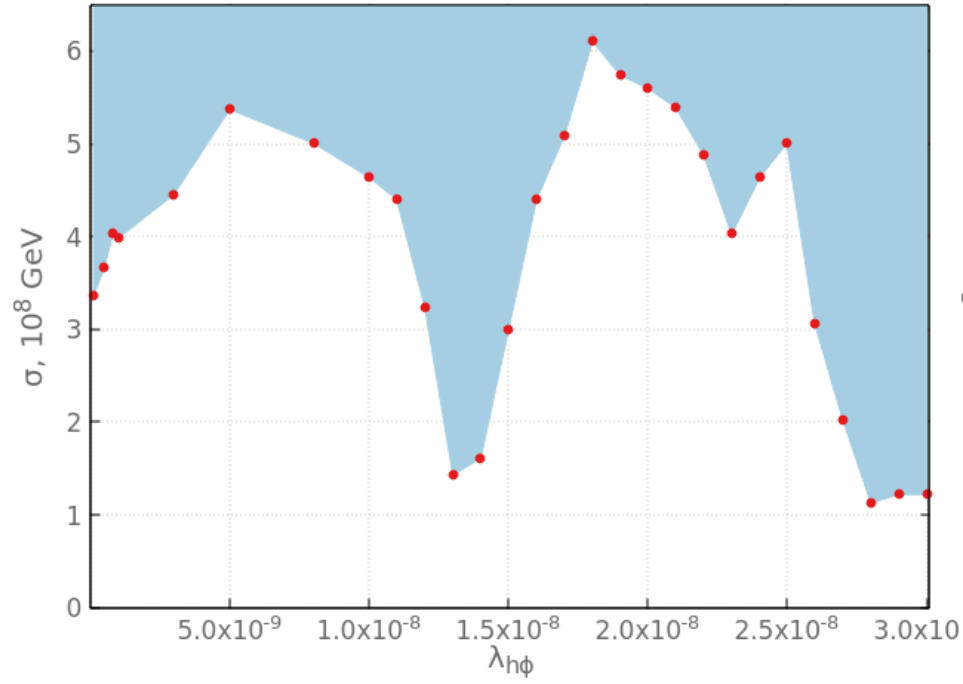
expansion of the universe \rightarrow in and out of the stability bands

example: $\lambda_h = 0$

- 1: $\sigma = 8 \times 10^{-11}$; $\lambda_{h\phi} = 1.5 \times 10^{-8}$;
- 2: $\sigma = -8 \times 10^{-11}$; $\lambda_{h\phi} = 1.5 \times 10^{-8}$;
- 3: $\sigma = 7 \times 10^{-11}$; $\lambda_{h\phi} = 2.5 \times 10^{-8}$;
- 4: $\sigma = 1 \times 10^{-11}$; $\lambda_{h\phi} = 3 \times 10^{-8}$;



instability regions, LATTICEEASY



shaded = excluded

CONCLUSION:

Inflationary Higgs fluctuations: tool to tackle

- Higgs vacuum instability

- Higgs-inflaton coupling